

## Homework, the 1st series

**Deadline: 5 April, 2013, 23:59**

Let  $Mult$  be the language of words over the alphabet  $\{0, 1, *, =\}$  of the form  $a * b = c$ , where  $a, b, c \in \{0, 1\}^*$  represent in binary some numbers  $A, B, C \in \mathbb{N}$ , such that  $A * B = C$ . For example  $11 * 101 = 1111$  is in the language and  $111 * 1 = 10$  is not.

Show that the language  $Mult$  can be recognized by a deterministic Turing machine working in space  $S(n) = \mathcal{O}(\log n)$  (where  $n$  is the length of the input word).